



Quantitative light microscopy of dense suspensions: Colloid science at the next decimal place

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Since the days of Perrin (1908) [1], microscopy methods have played an important role in the study of colloidal suspensions. Along with the continued development of new imaging techniques, colloid scientists have also implemented a sophisticated range of computational analyses. These analysis techniques are often the unsung heroes that hold the promise of unlocking scientific mysteries at the next decimal place of colloid science. They now enable precision measurements of particle location and size (Bierbaum et al., 2017; Kurita et al., 2012) as well as measurements of local stresses and forces (Lin et al., 2016). Here, we spotlight these exciting advances focusing on the analysis of simple brightfield and confocal microscope images of dense colloidal suspensions as well as the scientific mysteries they may unravel.

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Keywords:

Colloidal suspensions

Microscopy

Imaging

Forces

Measurement science

Current Opinion in Colloid & Interface Science (2018) 34, 32–46

This review comes from a themed issue on **Microscopy Methods**. For a complete overview see the [issue](#) and the [Editorial](#)

Article History:

Received 10 December 2017

Received in revised form 12 March 2018

Accepted 13 March 2018

Available online 23 March 2018

<https://doi.org/10.1016/j.cocis.2018.03.002>

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1. Introduction

“Why should one wish to make measurements with ever increasing precision? Because the whole history of physics proves that a new discovery is likely to be found lurking in the next decimal place.”

[(Floyd K. Richtmyer, 1931) [5]]

Look through a colloid scientist's microscope and you'll find an amazing array of phenomena that scientists and engineers investigate with colloidal suspensions. Particles entropically assemble into a zoo of crystal structures [6–11]. Aided by patterned substrates [12,13], gel coatings [14], depletion interactions [15–20], charge induced interactions [21–23], magnetic interactions [24–26] and DNA programmable interactions [27–30] the variety of accessible structures that suspensions form is breath taking. Active colloidal particles jet around, providing fertile testing grounds for far-from-equilibrium physics [31–36]. The behaviors of liquids [37,38], interfaces [39], gels [17,40,41] and glasses [42–47] are resolved with fine detail. Confocal rheoscopes illuminate the structural underpinnings of rheological behaviors from thixotropy [45,48,49] to shear thickening under confinement [50]. And the particles are no longer just spheres [51]; particle shapes have blossomed into a beautiful set of rods [52], clusters [24,53], dimers [54], lock-and-key particles [55], and even designed shapes from pentagons to letters [56–59], with simulations promising new materials from many of these shapes [60].

Simple microscopy methods such as brightfield and confocal are a large reason for the continued excitement in exploring such colloidal phenomena. The particles' large, micron-scale size and slow, millisecond- to second-scale dynamics allow key behaviors to be easily investigated by microscopy [19,44,46,61–65]. A modern microscope can image thousands of particles in a blink of an eye, and simple automated software routines can locate these particles to within 30 nm, while missing only a few percent of the

particles [66–68**]. Importantly, microscopy allows for local measurements of a suspension. Since particle interactions are often short ranged, the suspensions are frequently heterogeneous, and it is difficult to apply mean field concepts to understand their bulk behavior. Thus, the ability to image the local suspension structure has catalyzed a growth in the field, as theories that link local structures and their dynamics to the bulk suspension behavior can be tested on a per-particle level with statistically robust and well-controlled samples.

Yet some of the most interesting physical phenomena in colloidal science are not testable with traditional microscopy techniques. In typical experimental configurations, colloidal particles only deviate from hard-sphere interactions at nanometer separations. Numerous pioneering studies have elucidated how particle pairs interact at short distances [69–72]. However, measuring the strength of these interactions in dense suspensions, is difficult with the 30-nm localization accuracies of typical microscopy methods. For particles interacting *via* longer-range depletion forces, which occur on the 50–100 nm range, the bond energy can change greatly over the 30 nm uncertainty of typical approaches. Accurate localization is even more important for advancing studies of non-equilibrium colloidal matter, such as glasses and gels. Here, small changes in interparticle spacing can have huge effects on the macroscopic physics – a slightly tighter cage in a glass will have a much longer relaxation time, two particles slightly farther apart in a gel might no longer be bonded together. Worse, these systems are fundamentally heterogeneous, so there is little hope of inferring local properties of the material from scattering and bulk measurements. Moreover, since even the most monodisperse suspensions are not perfectly homogeneous [3], there is no guarantee that forces, stresses, or viscosities are homogeneous. Bulk methods such as rheometry cannot measure these local variations, while traditional microscopy cannot measure these mechanical properties at all. Finally, as particles with more complicated structure start to be synthesized more readily, it will become increasingly important to determine how these local properties depend on particle shape and size.

But over the past decade the situation has changed. With the advent of modern imaging techniques, faster computers to analyze the data, and the synergistic combination of the two, new techniques have been developed that are paving the way for a renaissance in the study of colloid suspensions. Today, research groups regularly acquire three-dimensional images of colloidal suspensions in real time. Coupled with careful analysis, these images provide a vast amount of information, yielding everything from nanometer-accurate position and size measurements [2**], shape information and orientation about non-spherical particles [52,73,74**], to even super-resolution images of individual particle microstructure [75*,76]. Just as exciting, researchers have found ways to use microscopes to measure stresses [4**], forces [77], and moduli [4**,78**]. Such techniques promise to fundamentally alter the toolbox available to scientists investigating suspensions.

In this article we highlight some of the more recent advances in the *analysis* of confocal and light microscopy

images of dense colloidal suspensions. Such analyses have had an enormous impact on colloid science but have received less attention than developments in microscopic imaging. There have, of course, been many exciting developments in microscopy over the past decade. For instance, there have been amazing developments in super-resolution imaging techniques including photoactivated localization microscopy (PALM) [79], stochastic optical reconstruction microscopy (STORM) [80], and stimulated emission depletion (STED) [81], as well as the continued development of ever more powerful techniques ranging from structured illumination [82] to lattice-light sheet [83] and Bessel Beam microscopy [84]. Another new set of techniques to keep an eye out for is holographic microscopy. While the idea of holography is old [85,86], recent improvements in the analysis of digital holograms have catapulted holography to the cutting edge of colloidal microscopy methods. For dilute suspensions, holography provides particle position, size, and even refractive index and shape with nanometer accuracy, from images captured with millisecond time resolution. Holographic microscopy excels for imaging single spheres [87–92*], clusters of spheres [93–95], rodlike colloidal particles [96,97], and even individual tracer particles in an otherwise un-imaged dense suspension [98*]. It can even be done on the cheap [99]. However, current methods are not yet able to accurately analyze holographic images of dense suspensions. As such, the application of holography to analyzing dense colloidal suspensions awaits further developments. Our focus on image analysis is based partly on practical criterion of space, but it is also based on a philosophical underpinning: New microscope imaging techniques can be expensive, whereas computers are cheap. Microscopes are costly to duplicate and require extensive maintenance, whereas software is easy to transfer from machine to machine and is practically maintenance-free. Why spend money buying new microscopes and complicated optics when you can improve the data you already have with better *inference* from the same images and analysis techniques that enable new science?

2. Better Inference

Since the landmark work by Crocker and Grier in the 1990s [66], colloidal science has relied heavily on automated particle tracking. The original Crocker-Grier routines in IDL can readily locate thousands of particles in microscope images and link the particles' trajectories through time, all in a few seconds. The ability to measure thousands of individual particle positions and to track those particles through time enables the testing of detailed microscopic theories, which has had a profound effect on colloidal science. It is because of particle tracking that we can visualize how crystals form and melt [62], understand how glasses rearrange and relax [44], and investigate the patterns formed in coffee rings as they dry [100]. Just as important, these particle tracking routines are easy to use, requiring no equipment other than a computer and an ordinary microscope, and requiring little extra training.

2.1. Centroid identification and related methods

The original particle location algorithm of Crocker and Grier [103] is now more than two decades old and still finds massive usage. Its permanence and effectiveness is due in a large part to its simplicity: it identifies particle positions as the intensity centroid of bright regions in an image. And due to its extensive usage, the original routine has been improved greatly by many people over the past two decades. Researchers have laid out how to take the best images for particle tracking [67,104]. Sources of bias, such as from anisotropic preprocessing kernels [105] or pixel bias [106–108], have been identified and diminished. Extensions to the algorithm can identify nearly all the particles in a field of view [68]. And, inspired by the original method, other algorithms have sprung up that can rapidly identify particle centers with little bias [109] or even for identifying particles that are not spheres, with shapes from rods to triangles being located [52,73,74,110,111].

However, the original Crocker-Grier method struggles with measuring particle sizes, and it has difficulty in measuring particle positions in size-polydisperse suspensions. Most particle location algorithms, including the method of Crocker and Grier, start by smoothing the image with a Gaussian blur to accentuate the particles (blob detection). But the optimal smoothing kernel size is tricky to find – use too small of a kernel and the image will be too noisy, use too big of a kernel and the particles will be blurred out into nothingness. Even worse, for samples with significant size polydispersity, an optimal kernel size might not exist. Leocmach and Tanaka [101] circumvent this problem of finding the correct kernel size by filtering the image repeatedly on many scales, a technique from computer vision known as a Scale Invariant Feature Transform or SIFT. Processing the image on a range of scales both enables particle identification in suspensions with polydisperse sizes and provides a way to measure the particle radii – the particle radius is the size at which the filter produces the maximal response (Fig. 1a–b). By using this technique to measure particle size in a size-polydisperse suspension, Leocmach and Tanaka [101] were able to measure the coupling between structural heterogeneity and particle size in super-cooled liquids (Fig. 1c), and they were able to show that smaller particles are expelled out of growing crystallites. However, while the method provides good relative sizing, it needs external calibration to give absolute particle radii measurements.

A conceptually similar approach is employed by Brujic et al. [112] to measure particle size. Rather than using SIFT by convolving the image with a Gaussian blob over a range of scales, Brujic et al. use deconvolution, by repeatedly deconvolving the image with the kernel of a sphere over a range of sphere radii. Since an image of a sphere can be viewed as a delta-function at the sphere's position convolved with a spherical kernel, the deconvolution of the image with a spherical kernel produces a series of spikes at the spheres' locations. This method gives the sphere's radii as well – the sphere's radii can be identified with the kernel whose radius produces the strongest response. Using this approach,

researchers have been able to characterize force networks and distributions [112] and the number of excess contacts [113] in jammed emulsion droplets.

But the most exciting new improvements to inference from images go beyond treating the particles as fuzzy bright blobs on the camera. Instead, they use additional information that the experimentalist knows about the image and the sample to greatly improve measurements of the recorded colloidal particles.

2.2. Inferring radii from positions

One such approach is to assume something about the relation between images over time. Combining fast but comparatively uninformative analysis methods, such as centroid-finding for particle positions, with a secondary analysis can not only increase precision, but can even provide new information.

A prime example of this idea is using only the measured particle positions to infer the particle radii [3,114]. Since approximate particle positions can be measured quickly, easily, and robustly, this inference technique provides a rapid way to back out individual particle radii. The algorithm infers the particle radii by assuming that the time-average surface-to-surface separation of one particle is the same as the time-average surface-to-surface separation in the entire sample. By tracking the center-to-center separation distance of all the particles in the image over time, and using the known sample-average surface-to-surface separation, Kurita and Weeks [3] can infer the individual particle radii from a time series (Fig. 1d). While it is not clear how good the assumption of equal separations is in general, Kurita et al. [3] have shown that the algorithm produces accurate results when fed simulated positions, such as positions of particles in a roughly monodisperse suspension, particles in a roughly bidisperse suspension, randomly-close-packed particles, and even of particles in a colloidal gel. In addition, they show that the experimentally measured radii distributions determined from their inference conform to a directly-measured size distribution from holography (Fig. 1e). From simulation data, they show that their indirect inference method can measure particle radii with an accuracy of either 0.5% of the particle's radius or 15% of the radii polydispersity, whichever is greater. Using these and related radii inference methods, researchers have shown that nucleation in 3D colloidal crystals tends to happen in regions of exceptionally high monodispersity [3], large particles in colloidal glasses have slower dynamics [115], and jammed suspensions of hard [114] or soft [102] spheres are hyperuniform (Fig. 1f).

While inferring particle radii solely from measured positions is rapid and easy to apply to existing datasets, its applicability is limited to systems where the assumption of equal average separation is valid. The original version of the algorithm assumes that the experimentalist knows the neighbor-averaged surface-to-surface separation, and that the average separation is the same for all particles on the time scale of the time series. In addition, the inferred radii could be biased if the errors in particle positions are

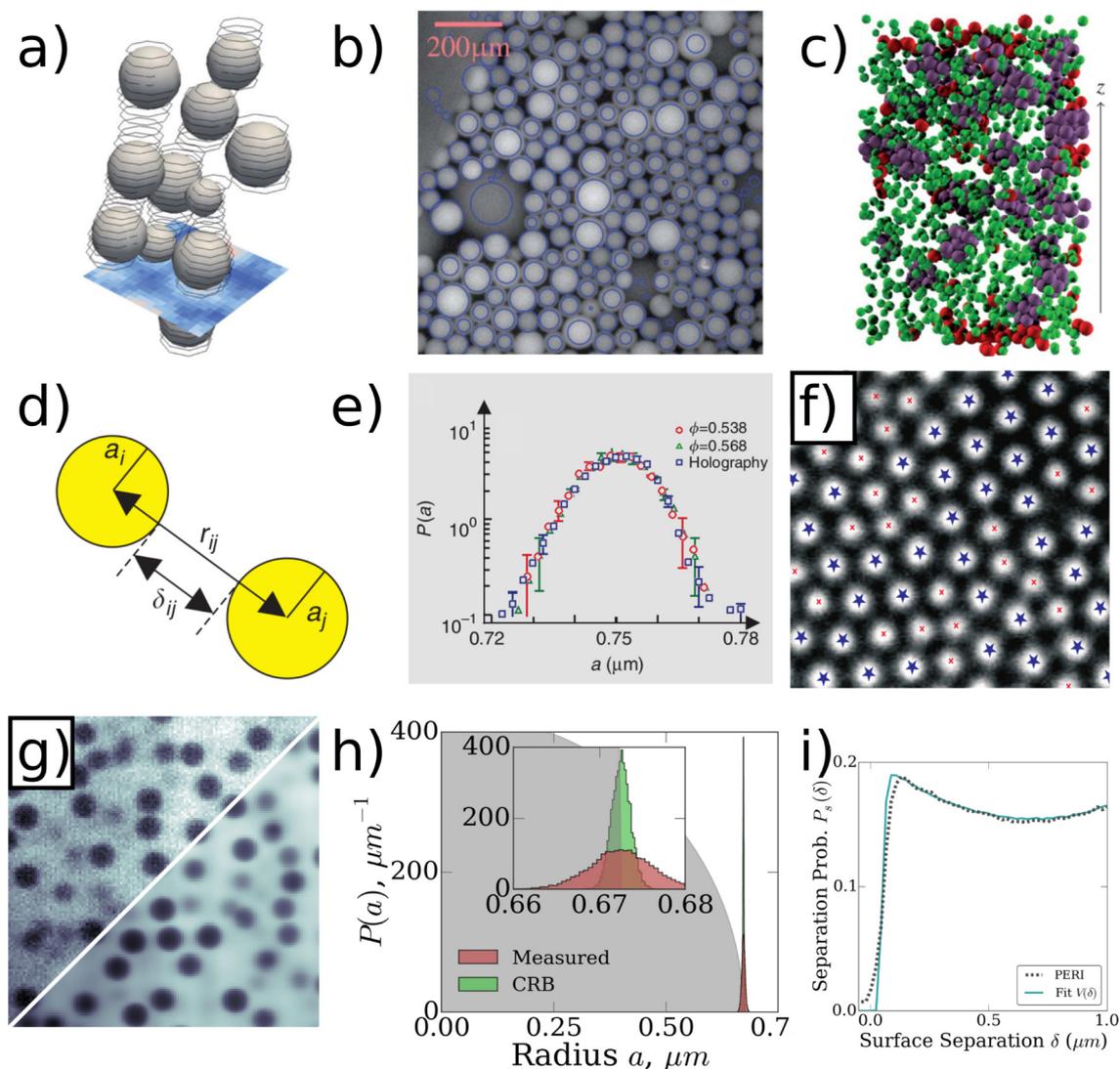


Fig. 1 Additional inference from images. *Multiscale method*: The multiscale method finds particle radii by the response to blob detection over a series of scale (a), which allows direct measurement of particle sizes (b). By looking at particle size distributions in a supercooled liquid (panel c), Leocmach and Tanaka showed that local icosahedral ordering (purple particles) centers around smaller (green) particles, and that crystal-like regions (red particles) do not occur near smaller particles. Adapted from ref. [101]. *Inferred Radii*: An alternative method to finding particle radii is to infer them from particle separations over a time series of images, assuming the average particle separation is the same throughout the sample (d). This provides easy access to particle radii, as shown by the agreement in particle size distributions compared to holography (e). By using this and similar methods, Dreyfus et al. were able to accurately measure hyperuniformity in jammed suspensions of size-bidisperse soft spheres (panel f, small and large particles as red and blue markers, respectively). Adapted from refs [3,102*]. *PERI*: PERI measures particle properties by generating a complete reconstruction of the entire image (panel g, raw data on left and reconstruction on right). The fitted parameters in the reconstruction provide accurate particles measurements, including particle radii to 3 nm (h). The accuracy is good enough to measure nm-scale interaction potentials (i).

correlated with the particle separation, which is the case for simple methods such as centroid-finding that do not account for blurring of the point-spread function. As such, inferring particle radii from the positions is best suited for long time series of homogeneous suspensions.

2.3. All the information

When extremely accurate measurements of particle positions and radii are needed for individual images, the most exact technique is PERI, or Parameter Extraction from Reconstructing

Images [2**]. PERI operates by fitting the image to a detailed, physically accurate, *in silico* model of the sample and the optical train, which creates a reconstruction of the entire image (Fig. 1g). Once the model, which includes everything from particle positions and sizes to aberrations in the microscope lens, accurately fits the experiment image, the fitted parameters are read out to get highly accurate inference on particle positions and sizes. In fact, when the physical model is complete and correct, PERI extracts *all* the useful information from the image: the unexplained portion of the data is only photon shot noise and the electronic noise of the detector. PERI can readily analyze three-dimensional images of thousands of particles, locating each and every particle's *position and radius* with accuracies of 1–3 nm in typical imaging conditions (Fig. 1h). By correctly accounting for optical diffraction and uneven illumination in the image, PERI can analyze images of dense suspensions without the significant bias present in other analysis techniques. The data are clean enough to measure interparticle interactions with a 10 nm range, even in a size-polydisperse suspension of spheres (Fig. 1i) [tebierbaum2017light](#). While the principle of PERI is general, it is currently only implemented for confocal images of colloidal particles, regardless of volume fraction.

The power of PERI comes at a price in computer time and user knowledge. While traditional methods for identifying particles, such as centroiding, can analyze a 3D image in a few seconds, PERI can take from 1 to 24 h to fit a complete image. Analyzing a time series of a few thousand separate images quickly becomes impractical on a single desktop computer. Fortunately, since the images are analyzed independently, this process is easily undertaken for each image in parallel on a cluster or supercomputer. With the advent of cheap cloud computing platforms such as Amazon Web Services, a researcher can spawn hundreds of processes at pennies on the compute-hour, allowing rapid and easy analysis of separate time series. Additionally, PERI works best when the microscope's optical train is accurately described. It remains to be seen how robust a given description of the optical train is across different microscopes and imaging variations. If the microscope's optical train is not well described by PERI, then the user will have to spend a considerable amount of time

implementing a detailed model of the microscope. Hopefully, as PERI matures these questions will be answered.

We provide a comparison of the aforementioned inference techniques in Table 1. While this list of particle position inference methods is by no means complete, it highlights some of the exciting developments and the range of analysis capabilities that are now readily accessible.

3. Using light microscopy to measure forces & stresses

This next decimal of precision in image analyses is also opening the door to measuring forces at the single particle scale. This capability is, in turn, enabling profound new scientific discoveries in colloid science. As a community we are now poised to understand in unprecedented detail how colloid based materials respond and evolve microscopically when they flow, yield, crack, creep, or even fracture.

Until recently, measurements of force and stress distributions were inaccessible in light or confocal microscopy of dense suspensions. Instead, microscopy has mainly been used to characterize the local suspension structure using, for example, pair correlation functions and various order parameters (Ψ_6 , Ψ_4 , etc.) as well as particle motions ranging from simple diffusion to cage hopping [44]. While these pioneering measurements have provided fruitful information about colloidal materials in liquid, crystal, glass, and gel phases, many scientific questions and debates remain because of the lack of information related to force distributions in these suspensions. Recently, however, new avenues for measuring such force and stress distributions have become available, through techniques such as local strain measurements, boundary stresses measurements, Stress Assessment from Local Structure Anisotropy (SALSA), phonon modes analyses, and microrheology. The underlying methodology of these techniques can be roughly divided into two categories: analysis based on elastic linear response (strain measurements and boundary stress microscopy) and statistical mechanics approaches (SALSA, phonon mode, and microrheology). Because of their different working mechanisms, these

Table 1 Comparison of inference methods for microscopy images.

	Centroiding [103,116,117]	Multiscale detection [101,118]	Inferred radii [3]	PERI [2**,119]
Analysis time	1 s	10 s	Not listed	1–24 h
Parallel computing?	Yes	Yes	No	Yes
Positional Accuracy	10–30 nm	~30 nm	n/a	1–3 nm
Radii accuracy	n/a	~0.1R	≤10 nm	3 nm
Assumptions	Qualitative	Qualitative	Long-time imaging, radii don't change	Optical train accurately described
Strengths	Simple and rapid	Simple relative radii measurement	Fast R	Highly accurate x, y, z, R measurement
Drawbacks	Inaccurate for dense suspensions	Calibration needed for absolute radii measurement	Radii & positional errors coupled	Long analysis time
Open source?	Yes	Yes	No	Yes

methods can also be used in combination to back out forces due to Brownian, hydrodynamic and contact interactions, as well as suspension viscosities [48,120*], and moduli [4*,78*].

3.1. Strain measurements

All solids display highly heterogeneous deformation fields when they yield. Therefore, understanding the local deformation or strain tensor and how it evolves under external loads is important to elucidating the nonlinear response of materials. The strain measurement technique calculates the local strain at a central particle from the neighboring particle displacements [5,47,63,121,122,133,134*,135–137]. The determined strain can then further be separated into affine and non-affine deformations. The non-affine part of the strain is critically relevant to the nonlinear response in yielded materials. The strain measurement technique has been used to study the defect nucleation dynamics in colloidal crystals [63], and the yielding mechanisms in glasses with specific focuses on the shear transformation zone [47,122,135] and Eshelby inclusions [121,122] (Fig. 2a). Importantly, however, the absolute strain relative to an undeformed lattice or configuration can only be determined for a crystalline suspension. Moreover, only the affine response can be related to the stress *via* a measurement of the modulus. In liquid or glassy suspensions the situation is further complicated by the fact that only relative strains are calculated. Whether these relax or further concentrate local stresses is difficult to interpret from experimental measurements of the strains alone.

3.2. Boundary stress microscopy

The mechanical response of soft materials can be highly heterogeneous. Measuring such spatial fluctuations of forces can provide valuable insights into the mechanisms that give rise to the extraordinary strengths of amorphous systems. Unfortunately, conventional microscopic flow measurements are only able to report the response that is averaged over a large area, glossing over many important microscopic features. Boundary stress microscopy however, visualizes these intriguing force patterns at the sample boundary [123*,124*] (Fig. 2b). This method shares the same principles as traction force microscopy but is applied to dense suspensions. Here, a thin layer of elastomer with embedded tracer particles is attached to the plate of a shear device (*e.g.* a rheometer or custom-made shear cell). When the loaded sample is sheared, its shear stress is then transmitted to the boundary and deforms the elastomer. By measuring the displacement of the tracer particles and the elastomer storage modulus, one can determine the spatial variation of the stress on the boundary. The main difference in philosophy with traction force microscopy is the focus on large surface regions and characterization of the inhomogeneous stress distributions.

Because the elastomer usually has excellent response properties, boundary stress microscopy is particularly useful for observing local stresses that can vary over many orders of magnitudes. For instance, it has been used to show that in a

collagen I gel, the local stress can exceed average stresses by an order of magnitude, with a length scale that is much larger than the fiber mesh [123*]. Furthermore, boundary stress microscopy has revealed dramatic spatial and temporal stress fluctuations in shear thickening suspensions. This evidence suggests that a shear thickening sample spontaneously and intermittently separates into different fluid phases with significantly different properties [124*].

3.3. Phonon mode measurements

While vibrational modes in colloidal crystals can be heavily damped by the surrounding solvent [138–141], it has been recently proposed that suspensions can still be used as a “shadow system” for calculating the properties of glassy systems. The idea is to start with the particle positions and to calculate the vibrational modes as though the particles were in a simple harmonic potential [125,126,129]. Using a normal mode analysis, the displacement covariance matrices of the particles are diagonalized to obtain the normal modes (Fig. 2c). Some numerical and experimental studies have extended the principal of density of state measurement to correlate the soft spots – regions with concentrated low-frequency vibrational modes – to the shear transformation zones and defects in glasses [127,142,143] and crystals [128,144], respectively. This analysis technique is particularly interesting since it represents a hybrid approach that combines experiments and simulations.

3.4. Microrheology

Mechanical rheometry is a long-standing standard method used to characterize the flow behavior of complex materials. However, conventional rheological measurements have several critical limitations, such as the need for relatively large sample volumes (on the order of a milliliter), the inability to characterize local mechanical heterogeneity, and low probing frequency due to instrument inertia. In the last few decades, microrheology has been developed and become a popular tool to overcome these challenges. In the original papers of microrheology [145,146], Mason and Weitz tracked the trajectories of the tracer particles in various of complex fluids, determined their mean square displacement (MSD), and, via the Stokes-Sutherland-Einstein relation, determined the material's complex modulus. While in principal, any methods that measure the particle MSD (*e.g.* Diffusing wave spectroscopy, dynamic light scattering, and fluorescence correlation spectroscopy) can be used for conducting microrheology, direct imaging has the advantage of providing valuable information about the spatial distribution of mechanical heterogeneity. Modern implementations of direct imaging include both measurement of tracer particle motions and differential dynamic microscopy [147*,148*,149].

Over time, many important improvements have been made. For example, two-point microrheology has been introduced to mitigate the artifacts arising from the tracer shape and size dependencies, as well as the coupling between the tracer and its embedded medium [150]. Optical tweezers [131], magnetic

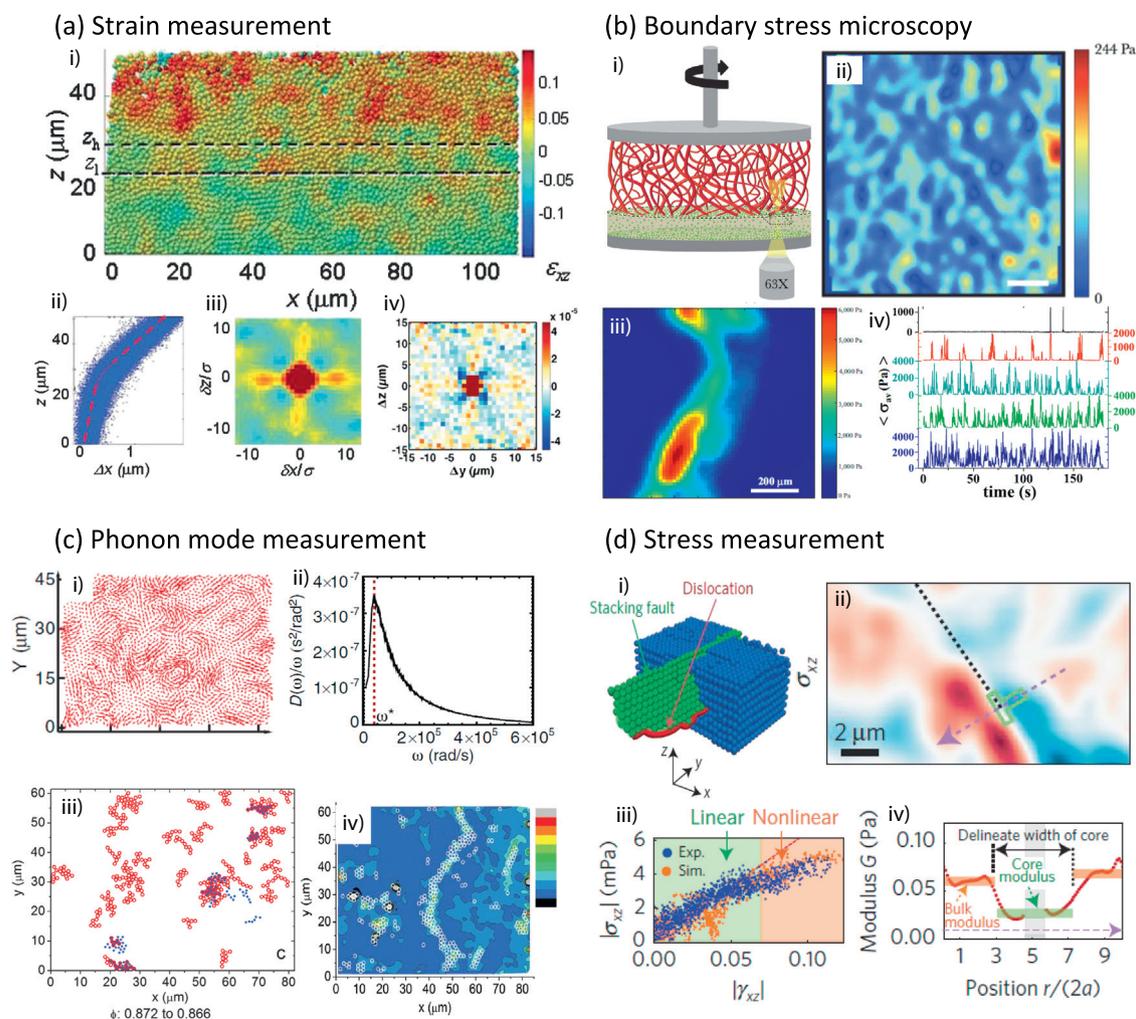


Fig. 2 Examples of mechanical measurements in colloidal suspensions: (a) i) Strain measurements show the shear banding behavior (red particles) in a sheared colloidal glass, as shown by the shear profile in ii) [121]. iii) The auto-correlation of the strain field exhibits a quadrupole pattern [121], consistent with the Eshelby inclusion model. iv) Surprisingly, similar correlation pattern has been found in quiescent colloidal glasses as well, suggesting that the thermal fluctuation can already trigger local structural transformations [122]. (b) i) Schematic of a boundary stress microscopy setup, where the bottom transparent plate is coated with an elastomer layer that contains tracer micro-particles [123^{**}]. ii) stress heterogeneities measured in a collagen I sample [123^{**}]. Spatial iii) and iv) temporal fluctuations of stresses in shear thickening suspensions [130^{*}]. (c) i) Phonon mode measurements visualize the normal mode in a colloidal glass [125]. ii) The measured density of state shows a clear boson peak feature [126]. iii) Soft spots determined using the phonon mode method in a sheared colloidal glass [127] and iv) a quiescent polycrystal [128]. (d) i) and ii) Stress field surrounding a dislocation measured by SALSA [4^{**}]. iii) and iv) by combining SALSA with the strain measurement, the local plasticity and modulus around the defect can be determined [4^{**}].

fields [132], and atomic force microscopes [130^{*}], have been implemented to drag tracers with forces much greater than thermal fluctuations, reaching the nonlinear response regime. In particular, to correctly link the measured nonlinear response to sample moduli, numerical models have been carried out to understand how the probe particle perturbs the sample's microstructure leading to corrections to the Stokes mobility [151–156]. Importantly, better particle location as described in Section 2 would improve these methods.

3.5. Local stress measurements

Another exciting development for measuring stresses in dense suspensions arises from adopting Irving and Kirkwood's idea [157], that determining forces is straightforward if the particle positions and interparticle potentials are known exquisitely. In particular, by summing the forces from neighboring particles one can determine the total force acting on any particle. This force distribution can then be smoothed

to determine the local stress. The situation is a bit more complicated for hard spheres since they only interact when particles collide with one another. Brady theoretically derived a formula to predict stresses in hard sphere suspensions based on calculation of the system averaged pair correlation function $g(\vec{r})$ [158]. The calculation relates the anisotropic particle distribution as measured by $g(\vec{r})$ to the suspension stress tensor. In 2010, Gao et al. [49] partially adopted this approach to experiments by measuring the pair correlation functions for flowing suspensions and comparing them to Stokesian Dynamics simulations. In 2011, Cheng et al. [48] implemented Brady's approach in full and showed that with experiments alone it is possible to extract the bulk stress from the pair correlation functions. This technique has gained rapid acceptance in the colloid community and is now implemented routinely by numerous groups [38,159,160].

In 2016, Lin et al. showed this macroscopic approach, can be generalized to the particle level. In particular, Stress Assessment from Local Structural Anisotropy (SALSA) measures the orientation distribution and probability of pairwise collisions between a particle and its nearest neighbors to determine the stresses arising from thermal collisions [4**]. SALSA has already been used to visualize the stress distributions surrounding crystal defects [4**] (See Fig. 2d) and the evolution of stresses in crystals under compression [78**]. Furthermore, SALSA has also been used to determine the viscosity of quiescent colloidal liquids by simply measuring thermally induced fluctuations of the shear stress [120*]. While current implementations have been used to investigate suspensions in the Brownian or low Péclet regime, it is likely that such measurements will also inform measurements of stress distributions under higher shear rates.

In Table 2 we provide a comparison of the range of techniques available for measuring forces. Once again, rather than a complete list, this table is meant to highlight the range of exciting techniques available for studying the heterogeneous mechanics in dense suspensions.

4. Application of analysis techniques to address long standing challenges in colloid science

The most exciting aspect of these novel analyses is the avenues that they open for investigating some of the most difficult problems in the science of suspension behaviors. Here, we sketch approaches for moving forward on a few of the science questions relating to crystals, glasses, gels, and shear thickening suspensions.

4.1. Crystals

Because of the relatively slow time scales associated with the particle motions, colloidal suspensions have been a valuable system for investigating a range of crystallization phenomena. In entropic crystals alone, these phenomena range from epitaxial growth [12,18] to defect nucleation and growth [13,63,161]. As colloidal systems become more sophisticated with different particle shapes [54,162] and

tunable interparticle potentials [19–30] understanding how the energetic driving forces alter rates of various processes will become increasingly important for making progress. Already, techniques for inferring local strains are making valuable contributions related to the role of substrate curvature to crystallization [3,163,164]. Local stress measurements have already shown the importance of nonlinear stresses surrounding defects [4**] and the role that squeeze flows induced by increased confinement have on the stress distribution in colloidal crystals [78**]. It is entirely conceivable that such measurements can also be used to determine the role of nonlinear stresses in driving defect dynamics, an exciting prospect for scientists hoping to develop design principles for guiding defect nucleation, propagation, and coalescence.

The ability to measure variations in particle radii presents another fascinating direction for studying the phase separation or crystallization of one particle species in the presence of another impurity or secondary phase. Already, it has been shown that for a nearly monodisperse suspensions, even slightly smaller particles end up accumulating at the boundaries of crystal grains [3] and that a low concentration of impurities can substantially alter crystallization [165]. The ability to determine the 3D position and size of a large number of secondary particles opens the door to investigations of how a secondary phase and the stresses it generates alter crystallization pathways and resulting kinetics, an increasingly important problem for which relatively few model systems exist [166].

4.2. Glasses

Colloids have been a cornerstone model system for investigating glassy phenomena. They have been instrumental in verifying concepts ranging from dynamic heterogeneity and cage hopping [42,44], to identifying soft spots associated with low order normal modes [127,142,143] and long range strain correlations associated with yielding [121,122,136]. Moving forward, there are many avenues for improving measurement techniques to usher in an understanding of glasses at “the next decimal place.” For example, most of the studies in colloidal glasses have been conducted with density-quenched monodisperse particles. This choice of system has been primarily dictated by experimental necessity – until recently it has been difficult to extract particle locations and sizes from images of dense polydisperse suspensions. But monodisperse suspensions locally crystallize, which makes them far from ideal for studying glassy behavior. The new inference techniques described in Table 1 now make it possible to easily investigate phenomena in bidisperse [3,46,167] and polydisperse suspensions [2**,3,101,112], determine volume fractions to much greater precision [2**], and even determine inhomogeneities in cage structure, which could elucidate whether the liquid to glass transition in colloids has the form of a Gardner transition with an increasingly fractal energy basin [168].

Additionally, much of the dynamic analysis of yielding in glassy suspensions has focused on measuring the magnitude

Table 2 Image-based methods for measuring mechanical properties of soft materials.

	Strain	Boundary stress	Phonon modes	Microrheology	Stress measurements (SALSA)
Mechanisms	Particle displacements	Tracers embedded in elastomer	Particle positions for calculating vibration modes	Passive: tracer's mean square displacement; Active: tracer's drag force	Inter-particle collision rate
Instrument modification	No	Elastomer coated on bottom substrate	No	Passive: no; Active: external field	No
Analysis challenges	Cannot infer nonlinear stress	Only shows stresses on the sample boundary; resolution bounded by tracer density	Requires long-time average to determine equilibrium positions; systematic errors from finite statistics [128]	Active: requires theoretical models for accurately interpreting nonlinear responses	Particle potential and collision criteria need careful validation
Sample limitation	Colloidal suspensions; only crystals allow force inferences relative to an undeformed lattice	None	None	Passive and active: tracer size must be taken into account	Inter-particle potential must be considered
Scientific finding examples	Shear transformation zones in colloidal glasses [47]; colloidal crystal defect nucleation dynamics [63]	Boundary stress inhomogeneities in shear thickening suspensions [124**] and bio-gels [123**]	Boson peaks and soft spots in colloidal glasses [125, 127, 129]	Passive and active: alternative method to rheometry for testing samples with small volume [130*, 131, 132]	Visualizing nonlinear stresses surrounding colloidal crystal defects [4**]

of and correlations in local relative strains [133]. Since there is no underlying lattice, it is not possible to define a strain in disordered suspensions. As such it is also not possible to determine whether the observed relative strains are relaxing or concentrating stresses. However, it should be possible to use techniques like boundary stress microscopy and SALSA to measure inhomogeneous stress distributions in sheared glasses and determine how they change under yielding. There are, of course, hurdles that remain. For example, the biggest difficulty with SALSA in a size-polydisperse suspension is to measure the particle positions and sizes with sufficient precision to accurately determine particle collisions probabilities. However, this particular hurdle can now be overcome by techniques like PERI. With such hurdles resolved, it should now be possible to observe how local stresses rearrange and percolate to enable the observed shear banding in yielding glasses [47].

4.3. Gels

Many of these improvements in measurement can also be applied to investigations of colloidal gels. In particular,

analyses in Table 1 can be used to track gels made out of polydisperse particles. Additionally, PERI can be used in conjunction with simulations to extract nm scale interparticle potentials [2**]. This enables the use of SALSA for measuring the individual particle stresses in colloidal gel networks with depletion or DLVO interparticle potentials. For the first time, we will be able to image and statistically catalog the percentage of structurally necessary force chains versus redundant internal force loops [169]. In combination with boundary stress microscopy it should be possible to determine how the structurally necessary boundary forces distribute within the bulk of the gel. This combination of measurements would garner a substantially deeper understanding of how the local structure of gels dictates their loading, yielding, and flow response.

Recently, excitement surrounding colloidal gel behavior has focused on the ability to embed a system-wide memory using oscillatory shearing protocols. By applying a given oscillatory strain, one can repeatedly break and reform the gel network until it can withstand a particular strain [170*, 171]. Measurements of local force inhomogeneities would also enable us to go much further in differentiating the properties associated with different regions of the gel responsible for maintaining rigidity versus those that enable plasticity and breakage. A

better understanding of these mechanisms will enable the formation of gels with properties that can be designed through various shear protocols.

4.4. Shear thickening

Colloidal suspensions also serve as an important model system for investigating non-Newtonian flows. These rheological phenomena include shear thickening at high strain rates, shear jamming of high suspension concentrations under rapid extensions, and solidification under rapid compression. There are many challenges in elucidating the microscopic origin for these behaviors. In shear thickening alone, there has been a vigorous and healthy debate relating to whether hydrodynamic or effective contact interactions between particles generate such behaviors [50,172–176*,177*]. Here too, the analyses we have described could play an important role in resolving such controversies. For example, using SALS in combination with force-sensitive dyes [77] it may be possible to determine the net force on a particle due to contact interactions. Alternatively, PERI could be used to determine interactions due to charge repulsion enabling measurement of effective contacts between particles. These contact and effective contact interactions are thought by many to determine shear thickening behavior in suspensions. The analyses described here would enable a more rigorous testing of these ideas. On larger length scales boundary stress microscopy is being used to identify phase inhomogeneities in shear-thickened suspensions [124**]. As the shear rate increases, the suspension forms regions of thickened material that grow in size, coalesce, and eventually take over the entire suspension. Such measurements illustrate the rich physics that must be understood on intermediate length scales in order to achieve sufficient understanding of these behaviors.

4.5. “... a new discovery is likely to be found lurking in the next decimal place”

The scientific problems and methodologies we have sketched here to address them are only a small taste of the new mysteries and scientific tool box developments to come. As new analyses are developed to complement the rapid expansion of microscope capabilities, it is likely that new science will be discovered, and with it new problems to address. One final idea that we would like to put forth is that future techniques will most likely make even more use of computation – not just to analyze images, but as an additional tool for experiments. For instance, in SALS computation is used to infer stresses based on estimation of interparticle collision probabilities. In phonon mode measurements, the colloidal suspension merely serves as a starting point for generating a computational model of a “shadow system.” And cheap computation can be used not only to generate model fits to images, as in PERI, but also to interpret the experimental data, such as fitting experimental data with a complete simulation to extract interparticle potentials [2**]. Such trends foreshadow an increasingly rich

range of creative approaches for making discoveries at “the next decimal place” of colloid science.

We thank Eric Weeks, Vinothan Manoharan, Roseanna Zia, and Mathieu Leocmach for helpful conversations in preparing this manuscript. This work was supported in part by National Science Foundation (NSF) Grant No. DMR-1507607 (I. C.), NSF Grant No. CBET-1509308 (N. L.), and ACS Grant No. PRF 56046-ND7 (B. L.).

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